

## 10.2 Exercises

Let  $f(x) = 3 + 2x$  and  $g(x) = x^2 - 2$ . Find the following.

- |                    |                    |                    |                     |
|--------------------|--------------------|--------------------|---------------------|
| 1. $f(1)$          | 2. $f(4)$          | 3. $g(2)$          | 4. $g(0)$           |
| 5. $g(-1)$         | 6. $g(-3)$         | 7. $f(-8)$         | 8. $f(-5)$          |
| 9. $f(-2) + f(-3)$ | 10. $f(1) + f(4)$  | 11. $g(1) + g(0)$  | 12. $g(-2) + g(-4)$ |
| 13. $g(5) + f(-1)$ | 14. $f(7) + g(-3)$ | 15. $f(-2) - g(1)$ | 16. $g(-5) - f(-1)$ |

Let  $f = \{(-1, 2), (0, 1), (1, 5), (2, 5)\}$  and  $g = \{(0, 4), (1, 3), (2, 2), (6, 1)\}$ . Find the following.

- |                   |                   |                   |                    |
|-------------------|-------------------|-------------------|--------------------|
| 17. $f(-1)$       | 18. $f(1)$        | 19. $g(0)$        | 20. $g(6)$         |
| 21. $g(6) + f(2)$ | 22. $f(0) - g(1)$ | 23. $f(0) - g(6)$ | 24. $g(2) - f(-1)$ |
| 25. $(f + g)(1)$  | 26. $(f + g)(2)$  | 27. $(fg)(2)$     | 28. $(fg)(1)$      |

Find an expression for  $f(x)$  in each of the following. Then find  $f(-2)$  and  $f(1)$ . See Example 2.

- |                   |                   |                   |                   |
|-------------------|-------------------|-------------------|-------------------|
| 29. $4x + y = 9$  | 30. $3x - y = 1$  | 31. $3x - 5y = 7$ | 32. $2x + 3y = 4$ |
| 33. $x^2 - y = 4$ | 34. $x^2 + y = 3$ | 35. $x = y^3$     | 36. $x + 2 = y^3$ |

Let  $f(x) = x^2 + 2x$  and  $g(x) = 2 + 7x$ . Find the following. See Example 4.

- |                   |                                   |                                    |                                   |
|-------------------|-----------------------------------|------------------------------------|-----------------------------------|
| 37. $(f + g)(2)$  | 38. $(f - g)(1)$                  | 39. $(fg)(0)$                      | 40. $\left(\frac{f}{g}\right)(1)$ |
| 41. $(f - g)(-3)$ | 42. $(fg)(-2)$                    | 43. $\left(\frac{f}{g}\right)(-2)$ | 44. $(fg)(3)$                     |
| 45. $(f + g)(r)$  | 46. $\left(\frac{f}{g}\right)(z)$ | 47. $(fg)(3z)$                     | 48. $(g - f)(5p)$                 |

Let  $f(x) = -x^2 + 2x + 1$  and  $g(x) = 4x - 3$ . Find the following. See Examples 3 and 5.

- |                      |                          |                          |                          |
|----------------------|--------------------------|--------------------------|--------------------------|
| 49. $f(r)$           | 50. $g(a)$               | 51. $f(z - 1)$           | 52. $f(2p + 1)$          |
| 53. $g(2q - 5)$      | 54. $(f \circ g)(-1)$    | 55. $(g \circ f)(0)$     | 56. $(g \circ f)(-2)$    |
| 57. $(f \circ g)(1)$ | 58. $(g \circ f)(2)$     | 59. $(g \circ f)(-3)$    | 60. $(f \circ g)(m)$     |
| 61. $(g \circ f)(r)$ | 62. $(g \circ f)(a + 2)$ | 63. $(f \circ g)(p + 1)$ | 64. $(g \circ f)(m + 1)$ |

In each of the following exercises, find (a)  $f(x + h)$ ; (b)  $f(x + h) - f(x)$ ; (c)  $\frac{f(x + h) - f(x)}{h}$ . (This quotient is important in calculus.) See Example 3.

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|-------------------------|------------------------|----------------------|----------------------|
| 65. $f(x) = 9x - 1$     | 66. $f(x) = 3x + 2$    | 67. $f(x) = 2x^2$    | 68. $f(x) = 5 - x^2$ |
| 69. $f(x) = -4x^2 + 6x$ | 70. $f(x) = 3x^2 - 5x$ | 71. $f(x) = 3 + x^3$ | 72. $f(x) = 1 - x^3$ |

In Exercises 73–76 write a function expressing the total cost  $C(x)$ , to manufacture  $x$  items.

73. The cost is \$7 per cheap watch.
74. \$12 is the cost to manufacture a basic calculator.
75. It costs a fixed \$5000 to set up a press to print a book, with an additional charge of \$2 per book printed.
76. A factory owner pays \$7200 to get the factory ready to make flower pots, with an additional charge of \$3 per pot.
77. A car rental agency charges \$35 plus 20¢ a mile (or a fraction of a mile) for a one-day rental. Let  $f(x)$  be the cost for a rental of  $x$  miles. Find the following.
- |                    |                                       |                                   |             |
|--------------------|---------------------------------------|-----------------------------------|-------------|
| (a) $f(8)$         | (b) $f\left(27\frac{1}{2}\right)$     | (c) $f\left(27\frac{3}{4}\right)$ | (d) $f(15)$ |
| (e) Graph $f(x)$ . | (f) Does $f(x)$ represent a function? |                                   |             |
78. The cost to rent a paint sprayer is \$3 per hour or portion of an hour, with a fixed \$2 cleaning charge. Let  $f(x)$  be the cost to rent a sprayer for  $x$  hours. Find the following.
- |                                       |              |              |                    |
|---------------------------------------|--------------|--------------|--------------------|
| (a) $f(1)$                            | (b) $f(3.8)$ | (c) $f(4.2)$ | (d) Graph $f(x)$ . |
| (e) Does $f(x)$ represent a function? |              |              |                    |

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1. 5      3. 2      5. -1      7. -13      9. -4      11. -3      13. 24      15. 0      17. 2  
 19. 4      21. 6      23. 0      25. 8      27. 10      29.  $f(x) = 9 - 4x; 17; 5$   
 31.  $f(x) = (3x - 7)/5; -13/5; -4/5$       33.  $f(x) = x^2 - 4; 0; -3$       35.  $f(x) = \sqrt[3]{x}; \sqrt[3]{-2}; 1$   
 37. 24      39. 0      41. 22      43. 0      45.  $r^2 + 9r + 2$       47.  $189z^3 + 144z^2 + 12z$   
 49.  $-r^2 + 2r + 1$       51.  $-z^2 + 4z - 2$       53.  $8q - 23$       55. 1      57. 2      59. -59  
 61.  $-4r^2 + 8r + 1$       63.  $-16p^2 + 2$       65. (a)  $9x + 9h - 1$  (b)  $9h$  (c) 9      67. (a)  $2x^2 + 4xh + 2h^2$  (b)  $4xh + 2h^2$  (c)  $4x + 2h$   
 69. (a)  $-4x^2 - 8xh - 4h^2 + 6x + 6h$  (b)  $-8xh - 4h^2 + 6h$  (c)  $-8x - 4h + 6$       71. (a)  $3 + x^3 + 3x^2h + 3xh^2 + h^3$  (b)  $3x^2h + 3xh^2 + h^3$   
 (c)  $3x^2 + 3xh + h^2$       73.  $C(x) = 7x$       75.  $C(x) = 5000 + 2x$       77. (a) \$36.60 (b) \$40.60  
 (c) \$40.60 (d) \$38.00 (e)  $f(x)$       (f) Yes