

[06-12-19-L11-A]

Questions before #47 intentionally omitted.

5.2 Radicals 215

5.2 Exercises

Write each of the following with radicals. Assume that all variables represent positive real numbers. See Example 3.

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|-------------------------|-------------------------|----------------------------|----------------------------|
| 47. $12^{1/2}$ | 48. $3^{1/2}$ | 49. $9^{1/5}$ | 50. $8^{3/4}$ |
| 51. $(7y)^{2/3}$ | 52. $(9q)^{5/8}$ | 53. $(3py^2)^{1/4}$ | 54. $(6a^2b)^{2/3}$ |
| 55. $(2m)^{-3/2}$ | 56. $(5y)^{-3/5}$ | 57. $(2y + x)^{2/3}$ | 58. $(r + 2z)^{1/2}$ |
| 59. $(p^2 + q^2)^{1/2}$ | 60. $(b^3 + a^3)^{1/3}$ | 61. $(3m^4 + 2k^2)^{-2/3}$ | 62. $(5x^2 + 3z^3)^{-5/6}$ |

Write with rational exponents. Assume that all variables represent positive real numbers. See Example 4.

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|---|---|----------------------------------|---|
| 63. $\sqrt{13}$ | 64. $\sqrt{29}$ | 65. $\sqrt[3]{7}$ | 66. $\sqrt[3]{24}$ |
| 67. $\sqrt{2^3}$ | 68. $\sqrt{5^5}$ | 69. $\sqrt[3]{6^4}$ | 70. $\sqrt[4]{7^3}$ |
| 71. $-\sqrt[3]{8^5}$ | 72. $-\sqrt[5]{9^2}$ | 73. $\sqrt[4]{x^3}$ | 74. $\sqrt[5]{y^3}$ |
| 75. $\sqrt[7]{a^2}$ | 76. $\sqrt[4]{p^9}$ | 77. $\frac{\sqrt{x^5}}{x^4}$ | 78. $\frac{\sqrt[3]{k^5}}{\sqrt[3]{k^7}}$ |
| 79. $\sqrt[4]{x^3} \cdot \sqrt[4]{x^6}$ | 80. $\sqrt[5]{y^2} \cdot \sqrt[5]{y^9}$ | 81. $\sqrt{m+r}$ | 82. $\sqrt{7z+2y}$ |
| 83. $\sqrt[4]{m^3+r^3}$ | 84. $\sqrt[5]{k^2}$ | 85. $\sqrt[3]{m-5n}$ | 86. $\sqrt[3]{8a-3b}$ |
| 87. $\sqrt[3]{9m^2p}$ | 88. $\sqrt[4]{12a^3b^2c}$ | 89. $2\sqrt{m} - 5\sqrt[3]{m^2}$ | 90. $3\sqrt[3]{p^2} + 2\sqrt[5]{p^3}$ |

Use absolute value to simplify each of the following. Assume that all radicands represent positive real numbers.

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|--|--|
| 91. $\sqrt{m^6}$ | 92. $\sqrt{r^{10}}$ |
| 93. $\sqrt{16z^2}$ | 94. $\sqrt{100p^2}$ |
| 95. $\sqrt{25r^4z^{10}}$ | 96. $\sqrt{64m^6n^8}$ |
| 97. $\sqrt{(r-2q)^2}$ | 98. $\sqrt{(3a-2b)^2}$ |
| 99. $\sqrt{m^2-2mq-q^2}$ | 100. $\sqrt{9z^2-24zx+16x^2}$ |
| 101. $\frac{-5}{\sqrt{p^4-2p^2q^2-q^4}}$ | 102. $\frac{3}{\sqrt{a^4-8a^2b+16a^2b^2}}$ |

Write Exercises 103–108 with rational exponents. Assume all variables represent positive real numbers.

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|-----------------------------------|-----------------------------|-------------------------------------|
| 103. $\sqrt{y} \cdot \sqrt[3]{y}$ | 104. $\sqrt[3]{xz}\sqrt{z}$ | 105. $\sqrt{\sqrt[3]{m}}$ |
| 106. $\sqrt[3]{\sqrt{k}}$ | 107. $\sqrt{\sqrt[3]{x^2}}$ | 108. $\sqrt[3]{\sqrt[5]{\sqrt{y}}}$ |

109. Show that $\frac{3 + \sqrt{3}}{3}$ is a solution of $3x^2 + 2 = 6x$.

110. Show that $\frac{-2 + 2\sqrt{11}}{5}$ is a solution of $5y^2 = 8 - 4y$.

Review Exercises Simplify each of the following. See Sections 3.1 and 3.2.

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|-----------------------------------|---|--|
| 111. $p^8 \cdot p^{-2} \cdot p^5$ | 112. $y^3 \cdot y^{-7} \cdot y^{-9}$ | 113. $(6x^2)^{-1}(2x^3)^{-2}$ |
| 114. $(5m^{-1})^2(3m^{-2})^{-1}$ | 115. $(8r^2s)^{-1}(2r^{-1}s^{-2})^{-1}$ | 116. $(3p^{-1}q^{-2})^{-1}(2pq^{-1})^{-1}$ |

Section 5.2 (page 214)

1. 9 3. 4 5. -6 7. 3 9. -5 11. Not a real number 13. -9 15. 2
 17. 4 19. -2 21. 4 23. -2 25. m^5 27. q^3 29. 6 31. 3
 33. 2.646 35. -4.359 37. -9.055 39. 12.247 41. -22.583 43. 29.833
 45. 6 square meters 47. $\sqrt{12}$ 49. $\sqrt[3]{9}$ 51. $\sqrt[3]{(7y)^2}$ or $\sqrt[3]{49y^2}$ 53. $\sqrt[4]{3py^2}$
 55. $1/\sqrt{(2m)^3}$ or $1/\sqrt{8m^3}$ 57. $\sqrt[3]{(2y+x)^2}$ 59. $\sqrt{p^2+q^2}$ 61. $1/\sqrt[3]{(3m^4+2k^2)^2}$
 63. $13^{1/2}$ 65. $7^{1/3}$ 67. $2^{3/2}$ 69. $6^{4/3}$ 71. $-8^{5/3}$ 73. $x^{3/4}$ 75. $a^{2/7}$

77. $x^{-3/2}$ 79. $x^{9/4}$ 81. $(m+r)^{1/2}$ 83. $(m^3+r^3)^{1/4}$ 85. $(m-5n)^{1/3}$ 87. $(9m^2p)^{1/3}$
 89. $2m^{1/2} - 5m^{2/3}$ 91. $|m^3|$ or $m^2|m|$ 93. $4|z|$ 95. $5r^2|z^5|$ or $5r^2z^4|z|$ 97. $|r-2q|$
 99. $|m-q|$ 101. $-5|p^2-q^2|$ 103. $y^{5/6}$ 105. $m^{1/6}$ 107. $x^{1/24}$ 111. p^{11}
 113. $1/(24x^8)$ 115. $s/(16r)$