

[07-04-15-T-8] Questions on Sets

List the elements of each set

1. The set of positive integers between 3 and 7.
2. The set of letters in the word "mississippi".
3. The set of major league baseball players who have batting averages of over .900.
4. The set of days of the week having names that begin with the letter "S".
5. The set of even numbers between 2 and 1000.
6. The set of odd numbers.

Say whether the statement is true or false.

7. $6 \in \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$
8. $\{5\} \in \{5, 10, 15, 20, \dots\}$
9. $10 \in \{2, 5, 8, 11, 13, 15, 20\}$
10. $22 \in \{x : x \text{ is an even number and less than } 18\}$
11. $\{1, 2, 3, 4, 5\} = \{0, 1, 2, 3, 4, 5\}$
12. $\{1\} \in \{1, \{1\}, 2, \{2\}, 3\}$

Let $\mathcal{A} = \{2, 4, 6, 8, 10, 12\}$

$\mathcal{B} = \{1, 3, 5, 7, 9, 11\}$

$\mathcal{C} = \{4, 6\}$

$\mathcal{D} = \{3, 5\}$

$\mathcal{E} = \{4, 5\}$

$\mathcal{F} = \{x : x \text{ is an odd number}\}$

$\mathcal{G} = \{x : x \text{ is an even number}\}$

Say whether the statement is true or false.

13. $\mathcal{A} \cap \mathcal{B} = \emptyset$
14. $\mathcal{C} \cap \mathcal{D} = \mathcal{E}$
15. $\mathcal{F} \cup \mathcal{G} = \mathcal{Z}^+$
16. $\mathcal{A} \cup \mathcal{C} = \mathcal{A}$
17. $\mathcal{A} \cap \mathcal{C} = \mathcal{C}$
18. $\mathcal{A} \subseteq \mathcal{A}$
19. $3 \subseteq \mathcal{B}$
20. $\mathcal{A} \subseteq \mathcal{F}$
21. $n\mathcal{A} = 4$
22. $n\emptyset = 1$
23. $\emptyset \subseteq \mathcal{D}$
24. $\emptyset \cap \mathcal{A} = \emptyset$

Write the following sets using set builder notation

25. $\{2, 4, 6, 8, \dots, 1000\}$
26. $\{1, 3, 5, \dots\}$

Questions 27, 28, 29, and 29, please **explain** why your answers are correct.

27. Suppose \mathcal{A} and \mathcal{B} are equivalent sets. Is $\mathcal{A} = \mathcal{B}$?
28. Suppose \mathcal{A} and \mathcal{B} are equal sets. Are \mathcal{A} and \mathcal{B} equivalent sets?
29. Does the set of even integers have the same number of elements as the set of integers?
30. Is it true that: if $x \in \mathcal{A}$ and $\mathcal{A} \subseteq \mathcal{B}$, then $x \in \mathcal{B}$?