

Summary of Differential Formulas and Corresponding Integrals

$$1. \frac{du}{dx} = \frac{du}{dx}$$

$$2. d(au) = a du$$

$$3. d(u + v) = du + dv$$

$$4. d(u^n) = nu^{n-1} du$$

$$5. d(\ln u) = \frac{du}{u}$$

$$6. \text{a) } d(e^u) = e^u du$$

$$\text{b) } d(a^u) = a^u \ln a du$$

$$7. d(\sin u) = \cos u du$$

$$8. d(\cos u) = -\sin u du$$

$$9. d(\tan u) = \sec^2 u du$$

$$10. d(\cot u) = -\csc^2 u du$$

$$11. d(\sec u) = \sec u \tan u du$$

$$12. d(\csc u) = -\csc u \cot u du$$

$$13. d(\sin^{-1} u) = \frac{du}{\sqrt{1-u^2}}$$

$$14. d(\cos^{-1} u) = \frac{-du}{\sqrt{1-u^2}}$$

$$15. d(\tan^{-1} u) = \frac{du}{1+u^2}$$

$$16. d(\cot^{-1} u) = \frac{-du}{1+u^2}$$

$$17. d(\sec^{-1} u) = \frac{du}{|u|\sqrt{u^2-1}}$$

$$18. d(\csc^{-1} u) = \frac{-du}{|u|\sqrt{u^2-1}}$$

$$1. \int du = u + C$$

$$2. \int a du = a \int du$$

$$3. \int (du + dv) = \int du + \int dv$$

$$4. \int u^n du = \frac{u^{n+1}}{n+1} + C, \quad n \neq -1$$

$$5. \int \frac{du}{u} = \ln |u| + C, \quad n = -1$$

$$6. \text{a) } \int e^u du = e^u + C$$

$$\text{b) } \int a^u du = \frac{a^u}{\ln a} + C$$

$$7. \int \cos u du = \sin u + C$$

$$8. \int \sin u du = -\cos u + C$$

$$9. \int \sec^2 u du = \tan u + C$$

$$10. \int \csc^2 u du = -\cot u + C$$

$$11. \int \sec u \tan u du = \sec u + C$$

$$12. \int \csc u \cot u du = -\csc u + C$$

$$13. \text{ and } \int \frac{du}{\sqrt{1-u^2}} = \begin{cases} \sin^{-1} u + C \\ -\cos^{-1} u + C \end{cases}$$

$$15. \text{ and } \int \frac{du}{1+u^2} = \begin{cases} \tan^{-1} u + C \\ -\cot^{-1} u + C \end{cases}$$

$$17. \text{ and } \int \frac{du}{u\sqrt{u^2-1}} = \begin{cases} \sec^{-1} |u| + C \\ -\csc^{-1} |u| + C \end{cases}$$

$$\int \sec u du = \ln |\sec u + \tan u|$$

$$\int \tan u du = -\ln |\cos u|$$